CPT INVARIANCE TESTS IN NEUTRAL KAON DECAY

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CPT theorem is based on three assumptions: quantum field theory, locality, and Lorentz invariance, and thus it is a fundamental probe of our basic understanding of particle

physics. Strangeness oscillation in
$$K^0-\overline{K}^0$$
 system, described by the equation
$$i\frac{d}{dt}\left[\frac{K^0}{K^0}\right]=[M-i\Gamma/2]\left[\frac{K^0}{K^0}\right]\ ,$$

where M and Γ are hermitian matrices (see PDG review [1], references [2,3], and KLOE paper [5] for notations and previous literature), allows a very accurate test of CPT symmetry;

indeed since CPT requires $M_{11} = M_{22}$ and $\Gamma_{11} = \Gamma_{22}$, the mass and width eigenstates, $K_{S,L}$, have a CPT-violating piece, δ , in addition to the usual CPT-conserving parameter ϵ :

$$K_{S,L} = \frac{1}{\sqrt{2(1+|\epsilon_{S,L}|^2)}} \left[(1+\epsilon_{S,L}) K^0 \pm (1-\epsilon_{S,L}) \overline{K}^0 \right]$$
$$-i\Im(M_{12}) - \frac{1}{2}\Im(\Gamma_{12}) \mp \frac{1}{2} \left[M_{11} - M_{22} - \frac{i}{2} (\Gamma_{11} - \Gamma_{22}) \right]$$

$$\epsilon_{S,L} = \frac{-i\Im(M_{12}) - \frac{1}{2}\Im(\Gamma_{12}) \mp \frac{1}{2} \left[M_{11} - M_{22} - \frac{i}{2} \left(\Gamma_{11} - \Gamma_{22} \right) \right]}{m_L - m_S + i(\Gamma_S - \Gamma_L)/2}$$

$$\equiv \epsilon \pm \delta. \tag{1}$$

Using the phase convention $\Im(\Gamma_{12}) = 0$, we determine the phase of ϵ to be $\varphi_{SW} \equiv \arctan \frac{2(m_L - m_S)}{\Gamma_S - \Gamma_L}$. Imposing unitarity to an arbitrary combination of K^0 and \overline{K}^0 wave functions, we obtain the Bell-Steinberger relation [4] connecting CP and CPT violation in the mass matrix to CP and CPT violation in

the decay; in fact, neglecting $\mathcal{O}(\epsilon)$ corrections to the coefficient

of the
$$CPT$$
-violating parameter, δ , we can write [5]
$$\left[\frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{\text{SW}}\right] \left[\frac{\Re(\epsilon)}{1 + |\epsilon|^2} - i\Im(\delta)\right] = \frac{1}{\Gamma_S - \Gamma_L} \sum_f A_L(f) A_S^*(f), \tag{2}$$

CITATION: C. Patrignani et al. (Particle Data Group), Chin. Phys. C, ${\bf 40}$, 100001 (2016) October 1, 2016 19:58 where $A_{L,S}(f) \equiv A(K_{L,S} \to f)$. We stress that this relation is phase-convention-independent. The advantage of the neutral kaon system is that only a few decay modes give significant contributions to the r.h.s. in Eq. (2); in fact, defining for the

hadronic modes

and the recent KLOE result [10])

$$\alpha_i \equiv \frac{1}{\Gamma_S} \langle \mathcal{A}_L(i) \mathcal{A}_S^*(i) \rangle = \eta_i \ \mathcal{B}(K_S \to i),$$

$$i = \pi^0 \pi^0, \pi^+ \pi^-(\gamma), 3\pi^0, \pi^0 \pi^+ \pi^-(\gamma), \tag{3}$$

the recent data from CPLEAR, KLOE, KTeV, and NA48 have led to the following determinations (the analysis described in Ref. 5 has been updated by using the recent measurements of K_L branching ratios from KTeV [6,7], NA48 [8,9], results described in the CP violation in K_L decays minireview,

$$\alpha_{\pi^{+}\pi^{-}} = ((1.112 \pm 0.010) + i(1.061 \pm 0.010)) \times 10^{-3} ,$$

$$\alpha_{\pi^{0}\pi^{0}} = ((0.493 \pm 0.005) + i(0.471 \pm 0.005)) \times 10^{-3} ,$$

$$\alpha_{\pi^{+}\pi^{-}\pi^{0}} = ((0 \pm 2) + i(0 \pm 2)) \times 10^{-6} ,$$

$$|\alpha_{\pi^{0}\pi^{0}\pi^{0}}| < 1.5 \times 10^{-6} \text{ at } 95\% \text{ CL } .$$

$$(4$$

(4)

The semileptonic contribution to the right-handed side of Eq. (2) requires the determination of several observables: we define [2,3]

$$\mathcal{A}(K^{0} \to \pi^{-}l^{+}\nu) = \mathcal{A}_{0}(1-y) ,$$

$$\mathcal{A}(K^{0} \to \pi^{+}l^{-}\nu) = \mathcal{A}_{0}^{*}(1+y^{*})(x_{+}-x_{-})^{*} ,$$

$$\mathcal{A}(\overline{K}^{0} \to \pi^{+}l^{-}\nu) = \mathcal{A}_{0}^{*}(1+y^{*}) ,$$

$$\mathcal{A}(\overline{K}^{0} \to \pi^{-}l^{+}\nu) = \mathcal{A}_{0}(1-y)(x_{+}+x_{-}) ,$$
(5)

where x_{+} (x_{-}) describes the violation of the $\Delta S = \Delta Q$ rule in CPT-conserving (violating) decay amplitudes, and yparametrizes CPT violation for $\Delta S = \Delta Q$ transitions. Taking advantage of their tagged $K^0(\overline{K}^0)$ beams, CPLEAR has measured $\Im(x_+)$, $\Re(x_-)$, $\Im(\delta)$, and $\Re(\delta)$ [11]. These determinations have been improved in Ref. 5 by including the information $A_S - A_L = 4[\Re(\delta) + \Re(x_-)]$, where $A_{L,S}$ are the

 K_L and K_S semileptonic charge asymmetries, respectively, from the PDG [12] and KLOE [13]. Here we are also including the T-violating asymmetry measurement from CPLEAR [14].

Table 1: Values, errors, and correlation co-

efficients for $\Re(\delta)$, $\Im(\delta)$, $\Re(x_{-})$, $\Im(x_{+})$, and $A_S + A_L$ obtained from a combined fit, including KLOE [5] and CPLEAR [14]. value Correlations coefficients

1

-0.21

1

 $(3.0 \pm 2.3) \times 10^{-4}$

 $(-0.66 \pm 0.65) \times 10^{-2}$

 $\sum_{\pi\ell\nu} \langle \mathcal{A}_L(\pi\ell\nu) \mathcal{A}_S^*(\pi\ell\nu) \rangle$

$$\Re(x_{-})$$
 $(-0.30 \pm 0.21) \times 10^{-2}$ -0.21 -0.60 1 $\Im(x_{+})$ $(0.02 \pm 0.22) \times 10^{-2}$ -0.38 -0.14 0.47 1 $A_{S} + A_{L}$ $(-0.40 \pm 0.83) \times 10^{-2}$ -0.10 -0.63 0.99 0.43 1 The value $A_{S} + A_{L}$ in Table 1 can be directly included in the semileptonic contributions to the Bell Steinberger relations in Eq. (2)

 $= 2\Gamma(K_L \to \pi \ell \nu)(\Re(\epsilon) - \Re(y) - i(\Im(x_+) + \Im(\delta)))$

 $= 2\Gamma(K_L \to \pi \ell \nu)((A_S + A_L)/4 - i(\Im(x_+) + \Im(\delta))) . (6)$

 $\alpha_{\pi\ell\nu} \equiv \frac{1}{\Gamma_S} \sum_{-\ell} \langle \mathcal{A}_L(\pi\ell\nu) \mathcal{A}_S^*(\pi\ell\nu) \rangle + 2i \frac{\tau_{K_S}}{\tau_{K_L}} \mathcal{B}(K_L \to \pi\ell\nu) \Im(\delta) ,$

Defining

 $\Re(\delta)$

 $\Im(\delta)$

 $\alpha_{\pi\ell\nu} = ((-0.2 \pm 0.5) + i(0.1 \pm 0.5)) \times 10^{-5}$.

Inserting the values of the
$$\alpha$$
 parameters into Eq. (2), we find

The complete information on Eq. (8) is given in Table 2.

(7)

(8)

October 1, 2016 19:58

 $\Re(\epsilon) = (161.1 \pm 0.5) \times 10^{-5},$

 $\Im(\delta) = (-0.7 \pm 1.4) \times 10^{-5}$.

Table 2: Summary of results: values, errors, and correlation coefficients for $\Re(\epsilon)$, $\Im(\delta)$, $\Re(\delta)$, and $\Re(x_{-})$.

	value	Correlations coefficients
$\Re(\epsilon)$	$(161.1 \pm 0.5) \times 10^{-5}$	+1
$\Im(\delta)$	$(-0.7 \pm 1.4) \times 10^{-5}$	+0.09 1
$\Re(\delta)$	$(2.4 \pm 2.3) \times 10^{-4}$	+0.08 -0.12 1
$\Re(x)$	$(-4.1 \pm 1.7) \times 10^{-3}$	+0.14 0.22 -0.43 1

Now the agreement with CPT conservation, $\Im(\delta) = \Re(\delta) = \Re(x_{-}) = 0$, is at 18% C.L.

The allowed region in the $\Re(\epsilon) - \Im(\delta)$ plane at 68% CL and 95% C.L. is shown in the top panel of Fig. 1.

The process giving the largest contribution to the size of the allowed region is $K_L \to \pi^+\pi^-$, through the uncertainty on ϕ_{+-} .

The limits on $\Im(\delta)$ and $\Re(\delta)$ can be used to constrain the $K^0-\overline{K}^0$ mass and width difference

$$\delta = \frac{i(m_{K^0} - m_{\overline{K}^0}) + \frac{1}{2}(\Gamma_{K^0} - \Gamma_{\overline{K}^0})}{\Gamma_S - \Gamma_L} \cos \phi_{SW} e^{i\phi_{SW}} [1 + \mathcal{O}(\epsilon)].$$

The allowed region in the $\Delta M = (m_{K^0} - m_{\overline{K}^0}), \Delta \Gamma = (\Gamma_{K^0} - \Gamma_{\overline{K}^0})$ plane is shown in the bottom panel of Fig. 1. As a result, we improve on the previous limits (see for instance, P.

Bloch in Ref. 12) and in the limit $\Gamma_{K^0} - \Gamma_{\overline{K}^0} = 0$ we obtain

 $-4.0\times 10^{-19}~{\rm GeV} < m_{K^0} - m_{\overline{K}^0} < 4.0\times 10^{-19}~{\rm GeV}~{\rm at}~95~\%~{\rm C}$

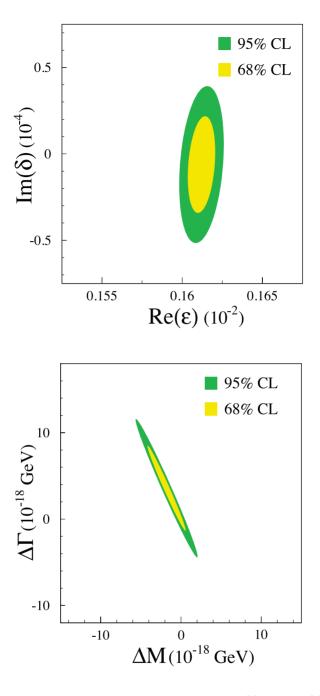


Figure 1: Top: allowed region at 68% and 95% C.L. in the $\Re(\epsilon)$, $\Im(\delta)$ plane. Bottom: allowed region at 68% and 95% C.L. in the $\Delta M, \Delta \Gamma$ plane.

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